

### 11.3 Vertex Form

To graph equations in standard form  $y = ax^2 + bx + c$ , one way is to complete the square to get into vertex form  $y = A(B(x-c))^2 + D$ .

Ex#1 Graph the following by converting to vertex form.

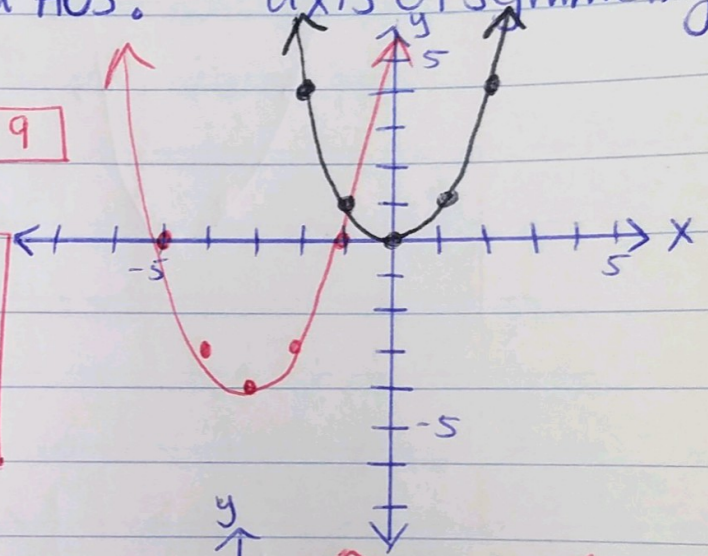
What are the vertex and AOS?  $\rightarrow$  axis of symmetry

a)  $g(x) = x^2 + 6x + 5$

$-5 + \boxed{9} = x^2 + 6x + \boxed{9}$

$4 = (x+3)^2$

$g(x) = (x+3)^2 - 4$   
 vertex:  $(-3, -4)$   
 AOS:  $x = -3$

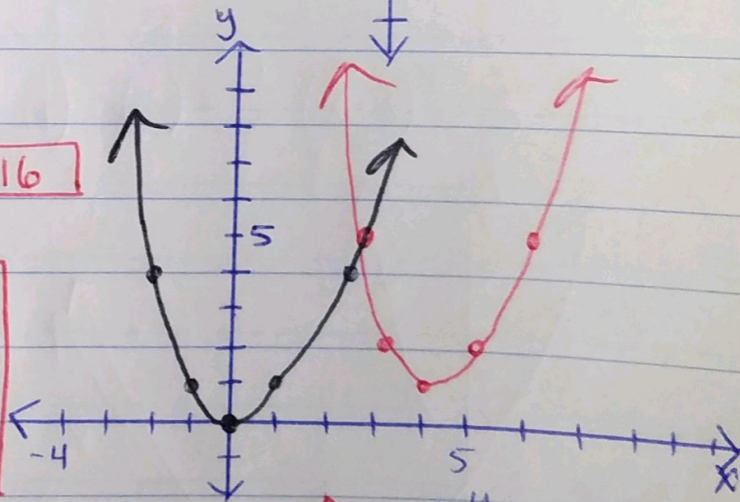


b)  $h(x) = x^2 - 8x + 17$

$-17 + \boxed{16} = x^2 - 8x + \boxed{16}$

$-1 = (x-4)^2$

$h(x) = (x-4)^2 + 1$   
 vertex:  $(4, 1)$   
 AOS:  $x = 4$



c)  $j(x) = 2x^2 + 4x + 5$

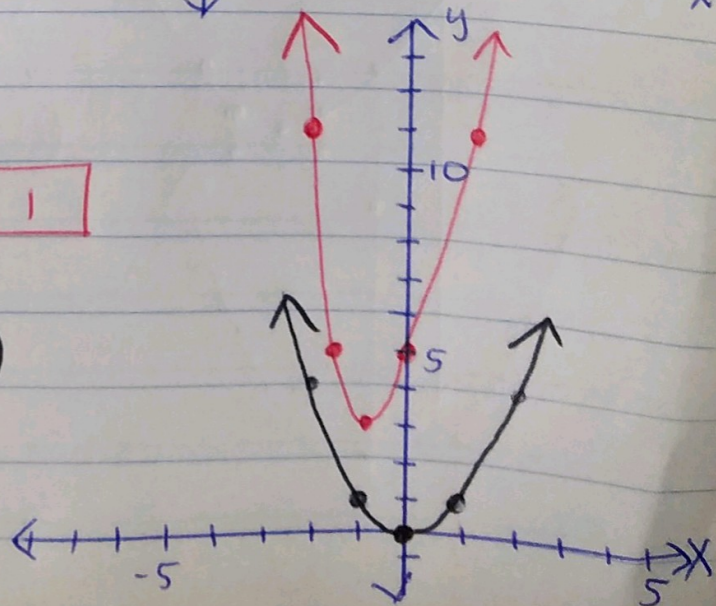
$\frac{j(x)}{2} = x^2 + 2x + \frac{5}{2}$

$-\frac{5}{2} + \boxed{1(\frac{2}{2})} = x^2 + 2x + \boxed{1}$

$-\frac{3}{2} = (x+1)^2$

$2 \left( \frac{j(x)}{2} = (x+1)^2 + \frac{3}{2} \right)$

$j(x) = 2(x+1)^2 + 3$   
 vertex:  $(-1, 3)$   
 AOS:  $x = -1$





$$d) k(x) = -3x^2 + 12x - 7$$

$$\frac{k(x)}{-3} = x^2 - 4x + \frac{7}{3}$$

$$-\frac{7}{3} + \boxed{4\left(\frac{3}{3}\right)} = x^2 - 4x + \boxed{4}$$

$$-\frac{7}{3} + \frac{12}{3} = (x-2)^2$$

$$\frac{5}{3} = (x-2)^2$$

$$\frac{k(x)}{-3} = (x-2)^2 - \frac{5}{3}$$

$$k(x) = -3(x-2)^2 + 5$$

vertex:  $(2, 5)$

AOS:  $x = 2$

