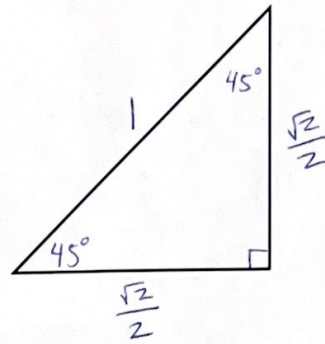
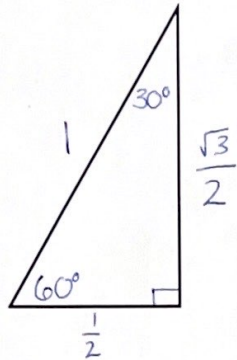


Special Triangles

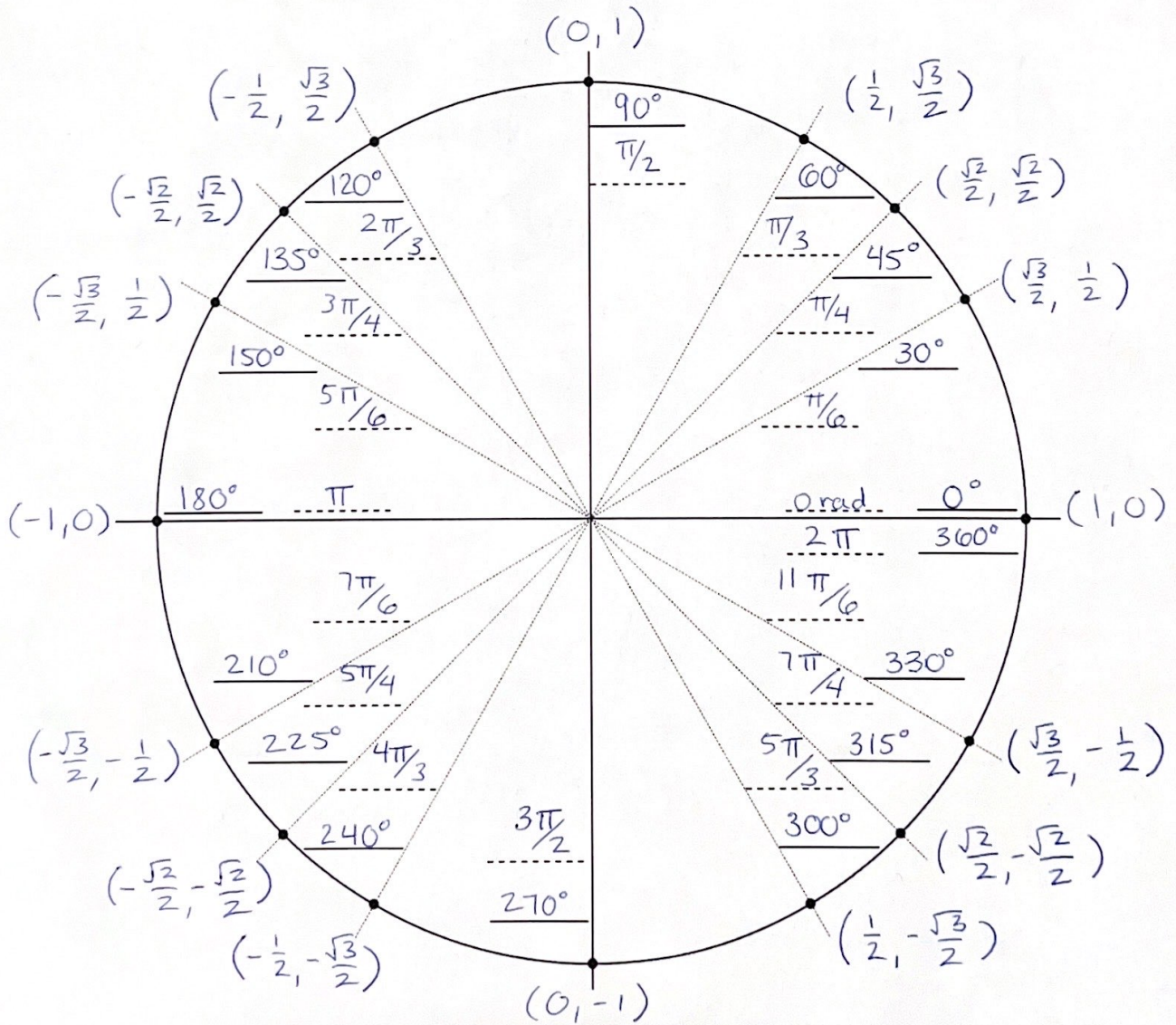


The Unit Circle

$\sin \theta = \frac{y}{r}$

$\cos \theta = \frac{x}{r}$

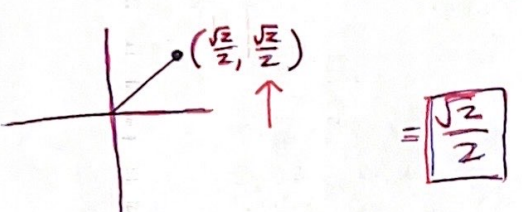
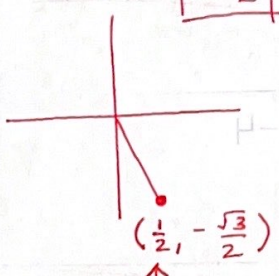
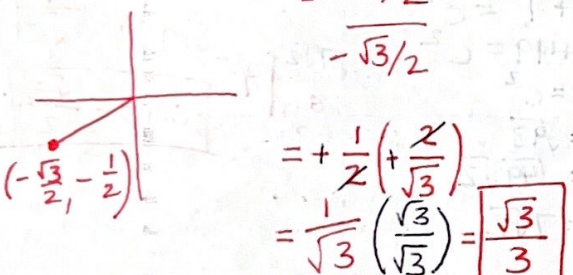
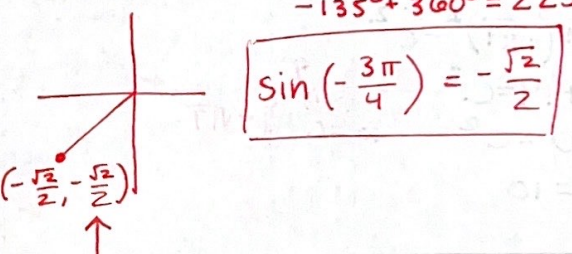
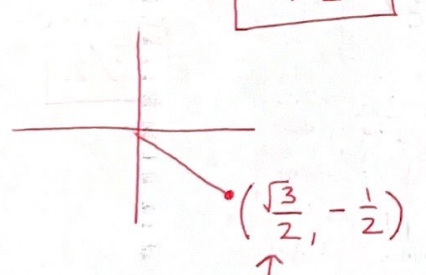
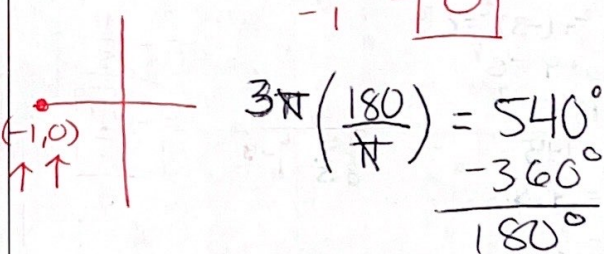
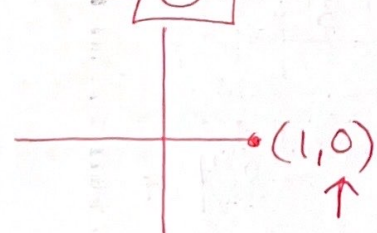
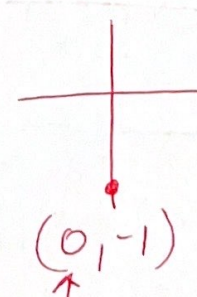
$\tan \theta = \frac{y}{x}$



Notes: 32.2 (continued) More on the Unit Circle

The Unit Circle

Use A66: Final Draft of the Unit Circle to complete the following.

<p>1. $\sin(-315^\circ)$ $= \sin(45^\circ)$</p> <p style="text-align: right;"> $\frac{-315^\circ + 360^\circ}{45^\circ}$ </p> 	<p>2. $\cos\left(\frac{5\pi}{3}\right) = \frac{1}{2}$</p> 
<p>3. $\tan 210^\circ$</p> <p style="text-align: right;"> $= -\frac{1/2}{-\sqrt{3}/2}$ $= +\frac{1}{\sqrt{3}} \left(\frac{2}{\sqrt{3}} \right)$ $= \frac{1}{\sqrt{3}} \left(\frac{\sqrt{3}}{\sqrt{3}} \right) = \frac{\sqrt{3}}{3}$ </p> 	<p>4. $\sin\left(-\frac{3\pi}{4}\right)$</p> <p style="text-align: right;"> $-\frac{3\pi}{4} \left(\frac{180}{\pi} \right) = -135^\circ$ $-135^\circ + 360^\circ = 225^\circ$ </p> <p style="text-align: right;"> $\sin\left(-\frac{3\pi}{4}\right) = -\frac{\sqrt{2}}{2}$ </p> 
<p>5. $\cos 330^\circ = \frac{\sqrt{3}}{2}$</p> 	<p>6. $\tan(3\pi) = \frac{0}{-1} = 0$</p> <p style="text-align: right;"> $3\pi \left(\frac{180}{\pi} \right) = 540^\circ$ $\frac{-360^\circ}{180^\circ}$ </p> 
<p>7. $\sin 0 = 0$</p> 	<p>8. $\cos \frac{3\pi}{2} = 0$</p> 

SOH-CAH-TOA

Trigonometry without The Unit Circle

- Make a triangle by dropping a perpendicular line to the x-axis.
- The angle near the origin/center is your reference angle.

Use the given point on the terminal side to find the value of the trig function indicated.

<p>9.</p> <p>$\cos \theta$</p> $a^2 + b^2 = c^2$ $3^2 + (-4)^2 = c^2$ $9 + 16 = c^2$ $25 = c^2$ $c = 5$ <p>$\cos \theta = \frac{3}{5}$</p>	<p>10.</p> <p>$\tan \theta = \frac{\sqrt{11}}{5}$</p>
<p>11.</p> <p>$\sin \theta$</p> $a^2 + b^2 = c^2$ $9^2 + (-\sqrt{19})^2 = c^2$ $81 + 19 = c^2$ $100 = c^2$ $c = 10$ <p>$\sin \theta = \frac{-\sqrt{19}}{10}$</p>	<p>12.</p> <p>$\sin \theta$</p> $7^2 + 7^2 = c^2$ $49 + 49 = c^2$ $98 = c^2$ $c = \sqrt{98}$ $c = \sqrt{49 \cdot 2}$ $c = 7\sqrt{2}$ <p>$\sin \theta = \frac{7}{7\sqrt{2}}$</p> <p>$\sin \theta = \frac{1}{\sqrt{2}} \left(\frac{\sqrt{2}}{\sqrt{2}} \right)$</p> <p>$\sin \theta = \frac{\sqrt{2}}{2}$</p>
<p>13.</p> <p>$\sin \theta$</p> $6^2 + (-3)^2 = c^2$ $36 + 9 = c^2$ $45 = c^2$ $c = \sqrt{45}$ $c = \sqrt{9 \cdot 5}$ $c = 3\sqrt{5}$ <p>$\sin \theta = \frac{-3}{3\sqrt{5}}$</p> <p>$= -\frac{1}{\sqrt{5}}$</p> <p>$= \frac{-\sqrt{5}}{5}$</p>	<p>14.</p> <p>$\tan \theta$</p> $(-2)^2 + (-\sqrt{5})^2 = c^2$ $4 + 5 = c^2$ $9 = c^2$ $c = 3$ <p>$\tan \theta = \frac{-\sqrt{5}}{-2}$</p> <p>$= \frac{\sqrt{5}}{2}$</p> <p>↑ don't need it!!!</p>
<p>15.</p> <p>$\cos \theta$</p> $(-\sqrt{19})^2 + (9)^2 = c^2$ $19 + 81 = c^2$ $100 = c^2$ $c = 10$ <p>$\cos \theta = \frac{-\sqrt{19}}{10}$</p>	<p>16.</p> <p>$\tan \theta = \frac{-\sqrt{7}}{3}$</p>