

## 21.4/21.5 More Exponential Transformations

### Exponential Transformations Review

$f(x) = (b)^x$  has the points:  $(-1, \frac{1}{b})$   $(0, 1)$   $(1, b)$

$f(x) = a(b)^x$  multiply the y-values of the points above by a

### Transformations

$$f(x) = a(b)^{x-c} + d$$

+c "c units left"  
 -c "c units right"  
 +d "d units up"  
 -d "d units down"  
 if negative "reflects over x-axis"  
 $|a| > 1$  "vertical stretch by  $|a|$ "  
 $|a| < 1$  "vertical shrink by  $|a|$ "

### **COMPLETE THE FOLLOWING ON THE GRAPH PAPER**

Ex #1: State the transformations, identify the asymptote, graph the function, and state the domain and range.

a) $f(x) = 3^{x+4} + 1$	b) $f(x) = 2\left(\frac{1}{3}\right)^x - 4$	c) $f(x) = \frac{1}{2}(4)^{x-4} - 2$
d) $f(x) = -3(2)^{x-6} + 5$	e) $f(x) = \frac{1}{2}(2)^{x-4} + 1$	f) $f(x) = -2\left(\frac{1}{3}\right)^{x+4}$

### Natural Base Exponential Functions

The natural number  $e$  (technically called Euler's number) comes up A LOT in Precalculus and Calculus when working with exponential functions, just like  $\pi$  comes up a lot in Geometry with circles.

$$(-1, \frac{1}{e}) (0, 1) (1, e) \rightarrow (-1, \frac{1}{e}) (0, 1) (1, e)$$

$$e \approx 2.71828\ldots$$

$$(-1, e) (0, 1) (1, e)$$

You can use  $\wedge\wedge\wedge$  that value instead of  $e$  in this class and always be correct.

### **COMPLETE THE FOLLOWING ON THE GRAPH PAPER**

Ex #2: State the transformations, identify the asymptote, graph the function, and state the domain and range.

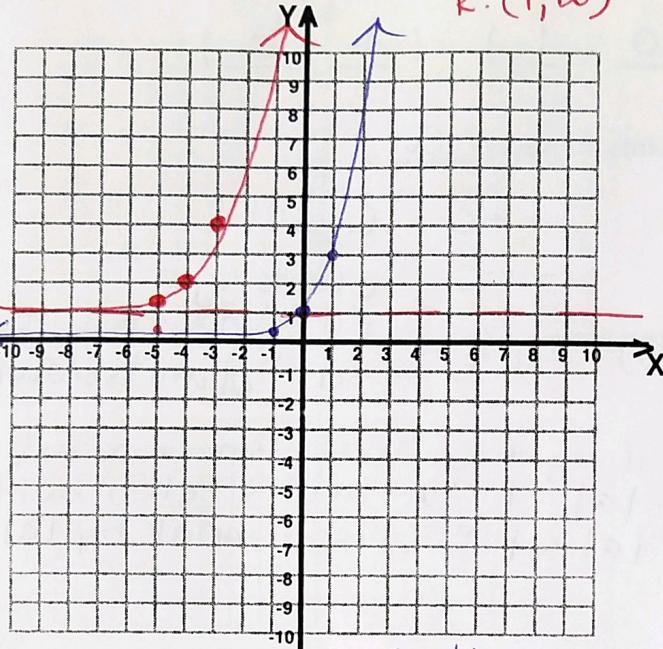
a) $f(x) = e^x$	b) $f(x) = -\frac{1}{2}e^x$	c) $f(x) = \frac{1}{4}e^x + 5$
d) $f(x) = e^{x-3} + 4$	e) $f(x) = -4e^{x-3} + 3$	f) $f(x) = 2e^{x+4}$

$$f(x) = 3^x$$

$$f(x) = 3^{x+4} + 1$$

4 left & 1 up  
 $y = 1$   
 D:  $(-\infty, \infty)$

$$R: (1, \infty)$$

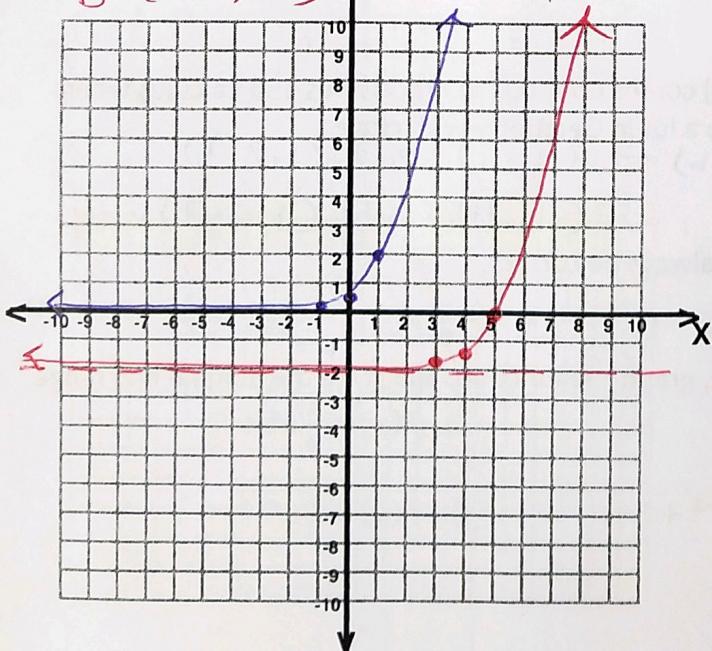


$$f(x) = \frac{1}{2}(4)^x$$

$$f(x) = \frac{1}{2}(4)^{x-4} - 2$$

vertical shrink by  $\frac{1}{2}$ , right 4, down 2  
 $y = -2$

$$D: (-\infty, \infty) \quad R: (-2, \infty)$$



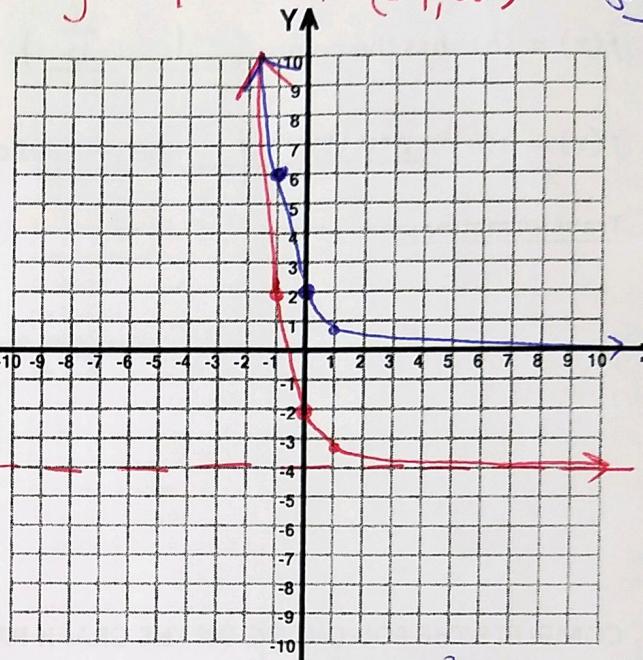
$$f(x) = 2\left(\frac{1}{3}\right)^x$$

$$f(x) = 2\left(\frac{1}{3}\right)^x - 4$$

vertical stretch by 2  
 & down 4  
 $y = -4$

$$D: (-\infty, \infty) \quad R: (-4, \infty)$$

$f(x) = 2\left(\frac{1}{3}\right)^x$   
 $f(x) = 2\left(\frac{1}{3}\right)^x - 4$   
 vertical stretch by 2  
 & down 4  
 $y = -4$   
 D:  $(-\infty, \infty)$   
 R:  $(-4, \infty)$   
 (win/wr)

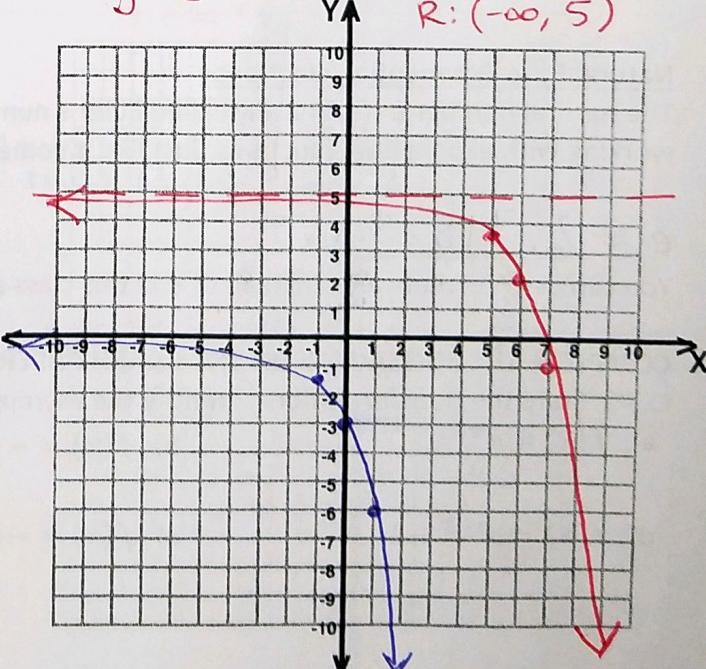


$$f(x) = -3(2)^x$$

$$f(x) = -3(2)^{x-6} + 5$$

reflect over x-axis, vertical stretch by 3,  
 right 6, up 5  
 $y = 5$

$$D: (-\infty, \infty) \quad R: (-\infty, 5)$$



$$f(x) = \frac{1}{2}(2)^x \quad (-1, \frac{1}{4}) \quad (0, \frac{1}{2}) \quad (1, 1)$$

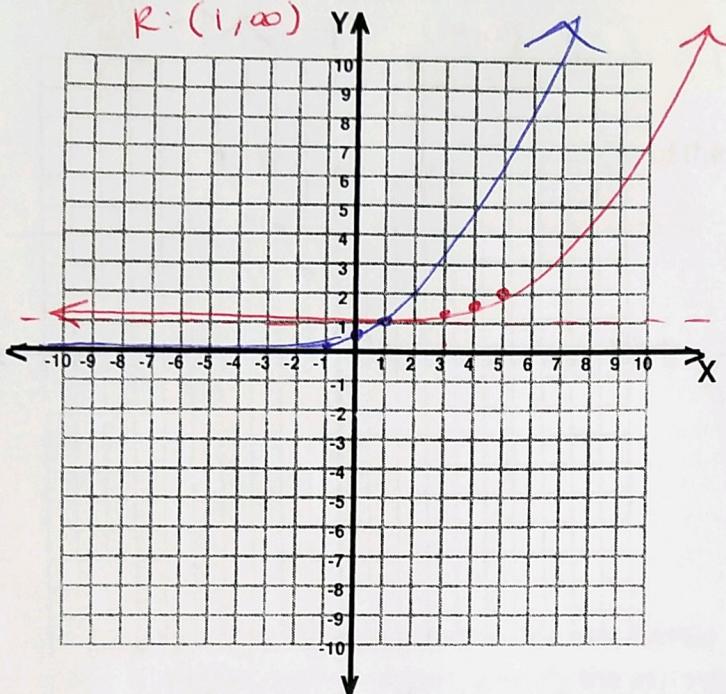
$$f(x) = \frac{1}{2}(2)^{x-4} + 1$$

vertical shrink by  $\frac{1}{2}$ , right 4, up 1

$$y = 1$$

$$D: (-\infty, \infty)$$

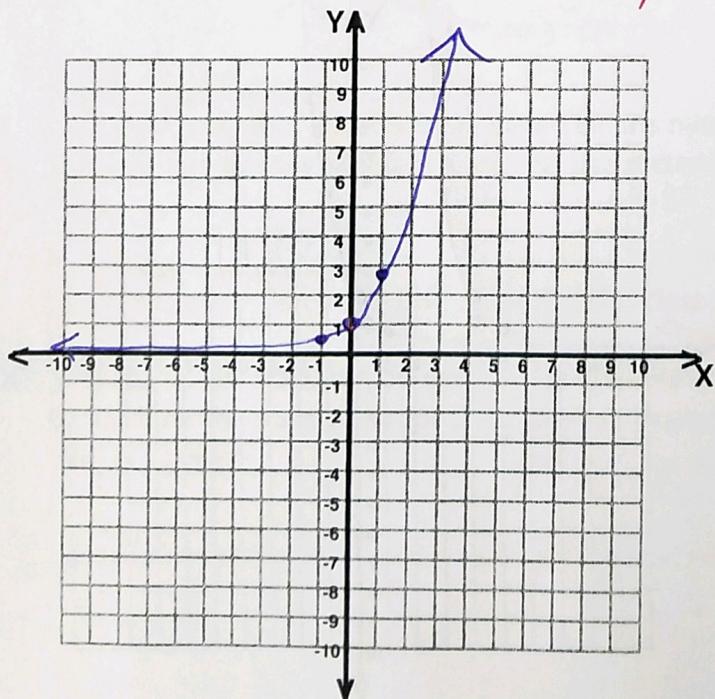
$$R: (1, \infty)$$



$$f(x) = e^x \quad (-1, .4) \quad (0, 1) \quad (1, 2.7)$$

NO transformations

$$y = 0 \quad D: (-\infty, \infty) \quad R: (0, \infty)$$



$$f(x) = -2(\frac{1}{3})^x \quad (-1, -6) \quad (0, -2) \quad (1, -\frac{1}{6})$$

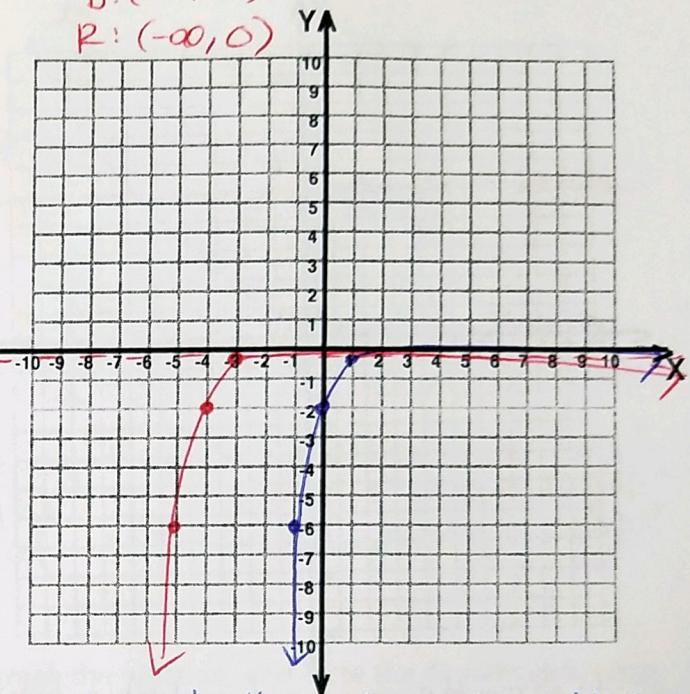
$$f(x) = -2(\frac{1}{3})^{x+4}$$

left 4, reflect over x-axis, vertical stretch by 2

$$y = 0$$

$$D: (-\infty, \infty)$$

$$R: (-\infty, 0)$$

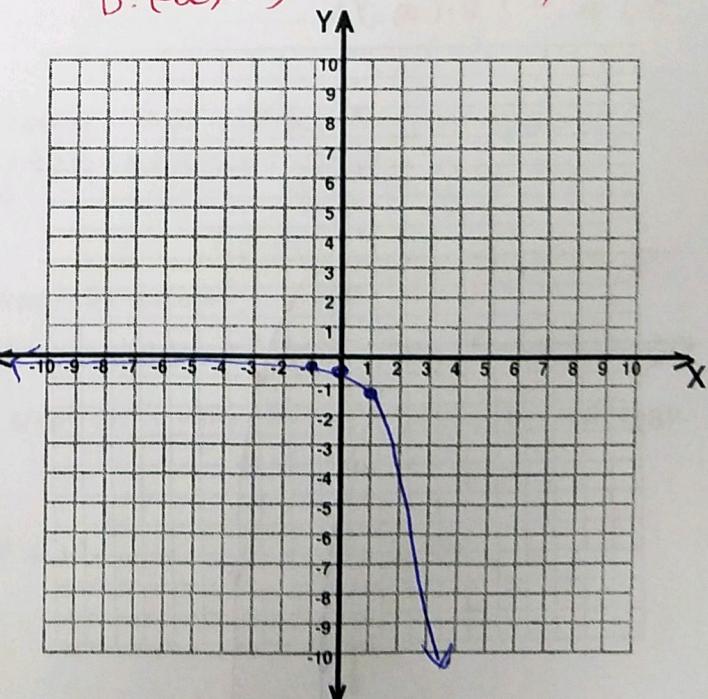


$$f(x) = -\frac{1}{2}e^x \quad (-1, -0.2) \quad (0, -\frac{1}{2}) \quad (1, -1.35)$$

reflection over x-axis, vert. shrink by  $\frac{1}{2}$

$$y = 0$$

$$D: (-\infty, \infty) \quad R: (-\infty, 0)$$

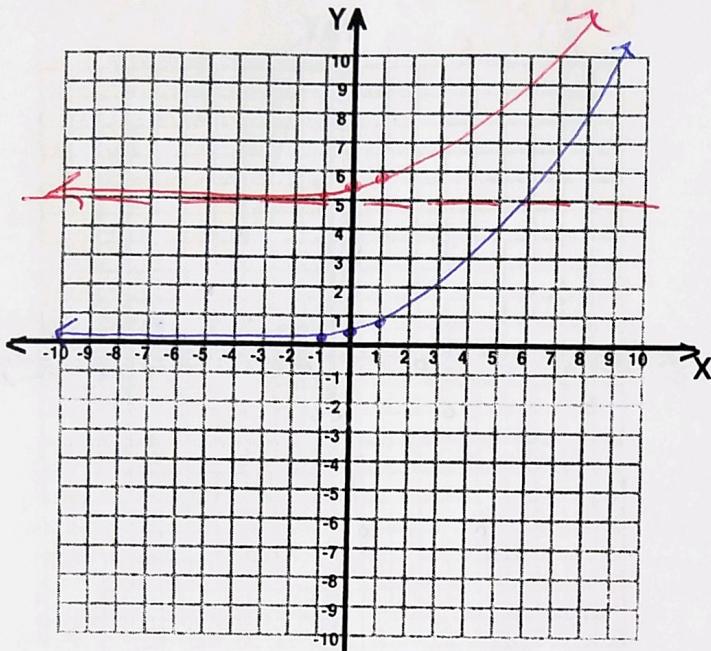


$$f(x) = \frac{1}{4}e^x \quad (-1, 1) \quad (0, \frac{1}{4}) \quad (1, 7)$$

$$f(x) = \frac{1}{4}e^x + 5$$

vertical shrink by  $\frac{1}{4}$ , up 5

$$y = 5 \quad D: (-\infty, \infty) \quad R: (5, \infty)$$



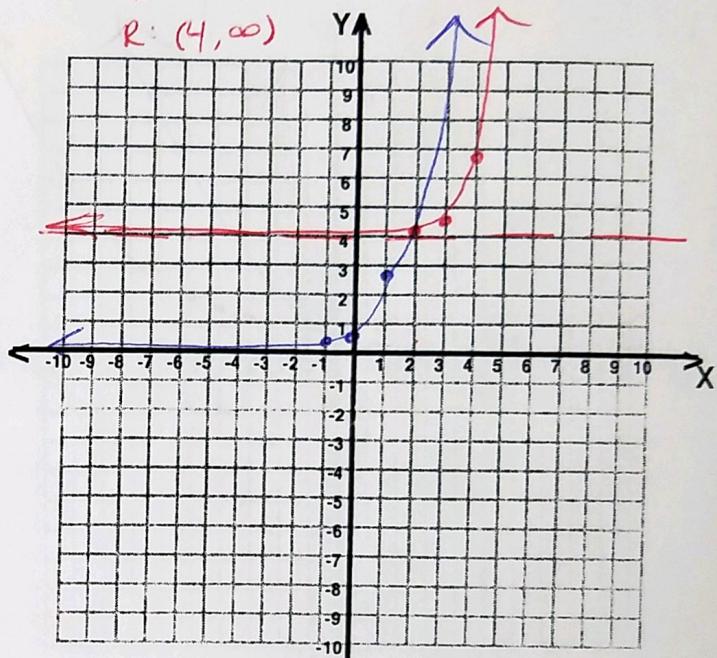
$$f(x) = e^x$$

$$f(x) = e^{x-3} + 4$$

right 3, up 4

$$y = 4$$

$$D: (-\infty, \infty)$$

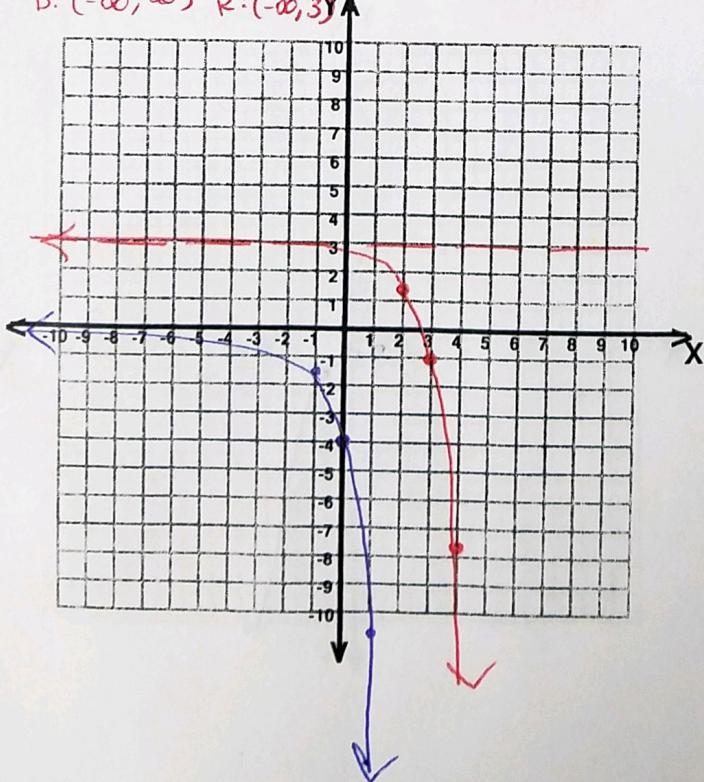


$$f(x) = -4e^x$$

$$f(x) = -4e^{x-3} + 3$$

reflect over x-axis, right 3, up 3,  
y = 3 vertical stretch by 4

$$D: (-\infty, \infty) \quad R: (-\infty, 3)$$



$$f(x) = 2e^x$$

$$f(x) = 2e^{x+4}$$

vertical stretch by 2, left 4

$$y = 0$$

$$R: (0, \infty)$$

