

22.2 The Common Logarithm Function

Common Logarithm - Has the form $y = \log(x)$ where $x > 0$.

$y = \log(x)$ can be rewritten as an exponent as $10^y = x$.

Ex #1 Turn the exponential equation into a logarithmic equation.

a) $10^4 = 10,000$ $\log 10,000 = 4$

b) $10^{-1} = \frac{1}{10}$ $\log \frac{1}{10} = -1$

c) $10^7 = 10,000,000$ $\log 10,000,000 = 7$

d) $10^0 = 1$ $\log 1 = 0$

e) $10^m = n$ $\log n = m$

Ex #2 Turn the logarithmic equation into an exponential equation.

a) $\log 100,000 = 5$ $10^5 = 100,000$

b) $\log \frac{1}{100} = -2$ $10^{-2} = \frac{1}{100}$

c) $\log 10 = 1$ $10^1 = 10$

d) $\log \frac{1}{1,000,000} = -6$ $10^{-6} = \frac{1}{1,000,000}$

e) $\log a = b$ $10^b = a$

Ex #3 Evaluate without a calculator.

a) $\log 1000 = ?$ $10^? = 1000$ $? = \boxed{3}$

b) $\log \frac{1}{10,000} = ?$ $10^? = \frac{1}{10,000}$ $? = \boxed{-4}$

c) $\log 10^6 = ?$ $10^? = 10^6$ $? = \boxed{6}$

d) $\log \frac{1}{1,000,000} = \boxed{-6}$

e) $\log \frac{1}{100} = \boxed{-2}$

Ex #4 Evaluate with a calculator.

a) $\log 3.7 \approx 0.568$

b) $\log \frac{1}{4} \approx -0.602$

c) $\log 0 = \text{Not a real \#}$

d) $\log 100 = 2$

e) $\log(-2) = \text{Not a real \#}$